

Zagazig University, Faculty of Engineering Midterm Exam

Academic Year: 2017/2018

Specialization: Computer & Systems Eng.

Course Name: Digital Control

Course Code: CSE421

Examiner: Dr. Mohammed Nour



Date: 11/11/2016

Exam Time: 60 min.

No. of Pages: 5

No. of Questions: 4 (20 items)

Full Mark: [60]

- ▷ Please answer all questions. Use 3 decimal digits approximation.
- ▷ Mark your answers for all questions in the Answer Sheet provided.
- ▷ In last page, some supplementary identities you *may* need.

Question 1

[2p] **1. Ballast Coding** is used to synchronize the sampling and control process. Which of the following does not apply for this method:

- completely implemented in software.
- software interrupt mechanism is used.
- adds dummy code to compensate for required sampling interval.
- very sensitive to changes in code and/or CPU clock rate.

[2p] **2.** For the two systems **A** and **B** represented by the following difference equations:

$$\mathbf{A} : y(k+2) = y(k+1)y(k) + u(k), \quad \mathbf{B} : y(k+5) = y(k+4) + u(k+1) - u(k),$$

- | | |
|--|--|
| a) A is homogeneous and B is linear. | b) A is time-variant and B is homogeneous. |
| c) both systems are linear and time-invariant. | d) both systems are time-invariant and homogeneous. |

[4p] **3.** The z-transform of the sequence: $\{0, 2^{-0.5}, 1, 2^{-0.5}, 0, 0, \dots\}$ is: (note: $\sin(45^\circ) = \frac{1}{\sqrt{2}}$)

- | | | | |
|------------------------------------|--|--|---|
| a) $\frac{z^2 + z + 1}{\sqrt{2}z}$ | b) $\frac{z^4 - 1}{z^3[z^2 - 2z + 1]}$ | c) $\frac{z}{[\sqrt{2}z^2 - 2z + \sqrt{2}]}$ | d) $\frac{z^4 - 1}{\sqrt{2}z^3[z^2 - \sqrt{2}z + 1]}$ |
|------------------------------------|--|--|---|

[4p] **4.** The inverse transform of the function: $F(z) = \frac{z}{z^2 + 0.3z + 0.02}$ is:

- a) $\{0, 1, -0.3, 0.07, \dots\}$ b) $\{1, -0.3, 0.07, \dots\}$ c) $\{0, 1, 0.3, 0.02, \dots\}$ d) $\{1, 0.3, 0.02, \dots\}$

[3p] **5.** The inverse transforms of the function: $F(z) = \frac{z - 0.1}{z^2 + 0.04z + 0.25}$ is:

- | | |
|--|---|
| a) $\sin(1.611k + 0.196)$ | b) $\cos(1.611k + 0.196)$ |
| c) $-0.4\delta(k) + 2.057(0.5)^k \sin(1.611k + 0.196)$ | d) $-0.4\delta(k) + \cos(1.611k + 0.196)$ |

[3p] **6.** If the discrete output y_k of a system is related to its input u_k by $y_n = \sum_{k=0}^n u_k$, the transfer function $Y(z)/U(z)$ of this system is:

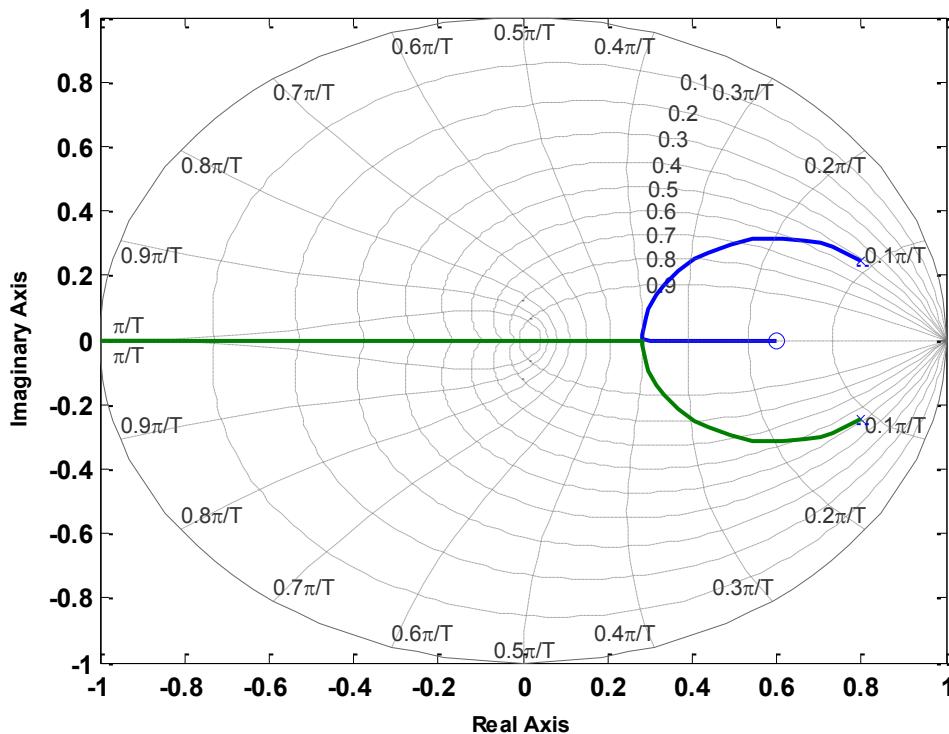
- | | | | |
|---------------------------|------------------------|------|-------------|
| a) $\frac{1}{1 - z^{-1}}$ | b) $\frac{z}{z^2 - 1}$ | c) 1 | d) z^{-1} |
|---------------------------|------------------------|------|-------------|

[3p] **7.** Consider a causal, LTI system with x_n and y_n as input and output, resp., described by the difference equation $y_n = a y_{n-1} + b x_n$. For which values of a and b is the system bounded-input bounded-output stable?

- a) $a > 1 \& b < 1$ b) $a < 1 \& b > 1$. c) $|b| < 1$ any a . d) $|a| < 1$, any b

Question 2

For the next questions, consider the next root Locus chart:



[3p] 8. The system represented by this root locus has a transfer function $G(z)$ given by:

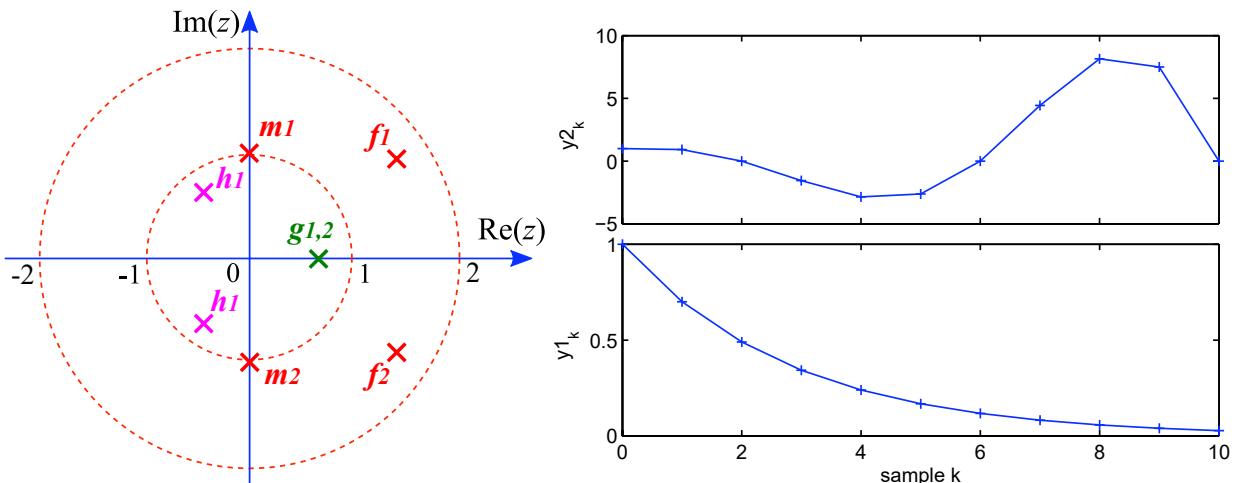
- a) $\frac{K(z^2 - 1.6z + 0.7)}{z - 0.6}$ b) $\frac{K(z - 0.6)}{z^2 - 1.6z + 0.7}$ c) $\frac{z - 0.4\pi/T}{(z^2 - 0.1\pi/Tz + 0.6)}$ d) $\frac{(z^2 - 0.1\pi/Tz + 0.6)}{z - 0.4\pi/T}$

[3p] 9. Using the given chart, the appropriate poles location that results in $\omega_n > 0.63$ rad/s, $\zeta > 0.8$ (assuming $T = 1$ s) are:

- a) $0.33 \pm j 0.17$ b) $0.17 \pm j 0.33$ c) $0.6 \pm j 0.2$ d) $0.2 \pm j 0.6$

Question 2

The following diagrams represent systems with poles (indicated by x's) but no zeros. The unit step response of two systems y_{1k} and y_{2k} is shown on the right plots.



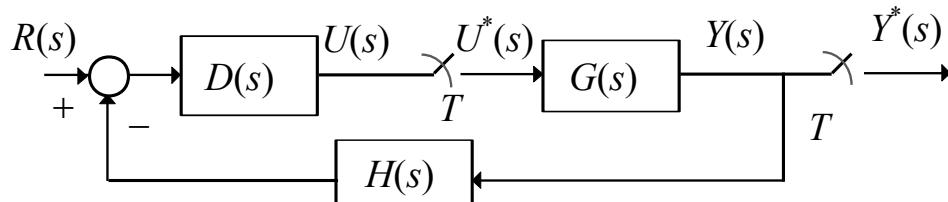
[3p] **10.**The system with the response given by y_{1k} has the poles:

- a) f_1, f_2 b) g_1, g_2 c) h_1, h_2 d) m_1, m_2

[3p] **11.**The system with the response given by y_{2k} has the poles:

- a) f_1, f_2 b) g_1, g_2 c) h_1, h_2 d) m_1, m_2

[3p] **12.**In the following sampled system, $D(s)$, $G(s)$, and $H(s)$ represent the system continuous subsystems. $R(s)$ and $Y(s)$ are input and output respectively:



The discrete response $Y(z)$ of this sampled system is:

- a) $Y(z) = \frac{G(z) DR(z)}{1 + D(z) HG(z)}$
 b) $Y(z) = \frac{G(z) D(z) R(z)}{1 + D(z) H(z) G(z)}$
 c) $Y(z) = \frac{G(z) D(z) R(z)}{1 + DHG(z)}$
 d) $Y(z) = \frac{G(z) DR(z)}{1 + DHG(z)}$

[3p] **13.**The final value for the function $F(z) = \frac{z}{z^2 + 0.3z + 2}$ is:

- a) 0 b) 3.3 c) 1/3.3 d) undefined

[3p] **14.**The steady state DC gain of the system with transfer Function $H(z) = \frac{z}{z^2 - 0.7z + 0.1}$ is:

- a) 0 b) 0.4 c) 2.5 d) undefined

[3p] **15.**For a system with the following characteristic equation:

$$F(z) = z^5 - 0.25z^4 + 0.1z^3 + 0.4z^2 + 0.3z - 0.1$$

The Jury Table constructed to determine this system stability will have:

- a) 5 rows b) 6 rows c) 7 rows d) 8 rows

[3p] **16.**The **filth** row of that Jury Table will be:

- a) -0.986 0.528 0.713 -0.528 b) 0.905 0.331 0.100 0.466
 c) 0.812 -0.2752 0.2288 d) 0.466 0.100 0.331 0.905

Question 3

In a unity feedback discrete system, its open loop transfer function is given as:

$$G(z) = \frac{k(0.084z^2 + 0.17z + 0.019)}{z^3 - 1.5z^2 + 0.553z - 0.05}$$

[3 p] 17. The system characteristic equation is:

- | | |
|-------------------|---------------------------------------|
| a) $G(z) = 0$ | b) $G(z) H(z) = 0$ |
| c) $1 + G(z) = 0$ | d) $z^3 - 1.5z^2 + 0.553z - 0.05 = 0$ |

[3 p] 18. The bilinear transformation used to transform the interior of the z-plane unit circle into the left-hand s-plane is:

- | | | | |
|----------------------|----------------------|-----------------|------------------|
| a) $\frac{1-w}{1+w}$ | b) $\frac{1+w}{1-w}$ | c) $z = e^{sT}$ | d) $z = e^{-sT}$ |
|----------------------|----------------------|-----------------|------------------|

[3 p] 19. The **third** row of the Routh–Hurwitz array will be:

- | | |
|---|--------------------------------------|
| a) $\frac{0.01k^2 - 1.55k + 4.17}{1.1 - 0.11k}$ | b) $1.1 - 0.11k \quad 3.1 + 0.07k$ |
| c) $3.1 + 0.07k$ | d) $0.003 + 0.27k \quad 3.8 - 0.27k$ |

[3 p] 20. Based on Routh–Hurwitz Criterion, this system is stable for k selected as:

- | | | | |
|----------------|-----------------|------------------------|---------------------|
| a) $k > -44.3$ | b) $k > -0.011$ | c) $-0.011 < k < 2.74$ | d) $-44.3 < k < 10$ |
|----------------|-----------------|------------------------|---------------------|

Supplementary Material

Note: you *may* need some or none of these identities:

No.	Property	Formula
1	Linearity	$\mathcal{Z}\{\alpha f_1(k) + \beta f_2(k)\} = \alpha F_1(z) + \beta F_2(z)$
2	Time Delay	$\mathcal{Z}\{f(k-n)\} = z^{-n}F(z)$
3	Time Advance	$\mathcal{Z}\{f(k+1)\} = zF(z) - f(0)$ $\mathcal{Z}\{f(k+n)\} = z^n F(z) - z^n f(0) - z^{n-1}f(1) \dots - z f(n-1)$
4	Discrete-Time Convolution	$\mathcal{Z}\{f_1(k)*f_2(k)\} = \mathcal{Z}\left\{\sum_{i=0}^k f_1(i)f_2(k-i)\right\} = F_1(z)F_2(z)$
5	Multiplication by Exponential	$\mathcal{Z}\{a^{-k}f(k)\} = F(az)$
6	Complex Differentiation	$\mathcal{Z}\{k^m f(k)\} = \left(-z \frac{d}{dz}\right)^m F(z)$
7	Final Value Theorem	$f(\infty) = \mathcal{Z}_{k \rightarrow \infty} f(k) = \mathcal{Z}_{z \rightarrow 1} (1 - z^{-1})F(z) = \mathcal{Z}_{z \rightarrow 1} (z-1)F(z)$
8	Initial Value Theorem	$f(0) = \mathcal{Z}_{k \rightarrow 0} f(k) = \mathcal{Z}_{z \rightarrow \infty} F(z)$

$$\begin{aligned}
 e^{jx} &= \cos x + j \sin x, \\
 \cos x &= \frac{e^{jx} + e^{-jx}}{2}, \quad \sin x = \frac{e^{jx} - e^{-jx}}{2j} \\
 x + jy &= \sqrt{x^2 + y^2} \quad e^{j \tan^{-1}(y/x)} \\
 G(s) &= \frac{\omega_n^2}{s^2 + 2\xi\omega_n s + \omega_n^2}, \quad \omega_d = \omega_n \sqrt{1 - \xi^2} \\
 T_r &= \frac{\pi - \beta}{\omega_d}, \quad \beta = \tan^{-1} \frac{\omega_d}{\xi\omega_n}, \quad T_p = \frac{\pi}{\omega_d}, \\
 T_s &= \left. \frac{3}{\xi\omega_n} \right|_{5\%} = \left. \frac{4}{\xi\omega_n} \right|_{2\%}, \quad M_p = e^{-\xi\pi/\sqrt{1-\xi^2}} \\
 k_0 &= K_p \left(1 + \frac{T}{T_i} + \frac{T_d}{T} \right), k_1 = -K_p \left(1 + 2 \frac{T_d}{T} \right), \\
 k_2 &= K_p \left(\frac{T_d}{T} \right) \\
 \Phi &= e^{Ah} = \mathcal{L}^{-1} \left\{ (sI - A)^{-1} \right\}, \Gamma = \int_{t=0}^h e^{At} B dt
 \end{aligned}$$

التاريخ : / /

اسم الطالب :

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عشرات										
مئات										
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ختم الكترون



No.	Continuous Time	Laplace Transform	Discrete Time	z-Transform
1	$\delta(t)$	1	$\delta(k)$	1
2	$1(t)$	$\frac{1}{s}$	$1(k)$	$\frac{z}{z-1}$
3	t	$\frac{1}{s^2}$	kT	$\frac{zT}{(z-1)^2}$
4	t^2	$\frac{2!}{s^3}$	$(kT)^2$	$\frac{z(z+1)T^2}{(z-1)^3}$
5	t^3	$\frac{3!}{s^4}$	$(kT)^3$	$\frac{z(z^2+4z+1)T^3}{(z-1)^4}$
6	$e^{-\alpha t}$	$\frac{1}{s+\alpha}$	a^k	$\frac{z}{z-a}$ by setting $a = e^{-\alpha T}$.
7	$1 - e^{-\alpha t}$	$\frac{\alpha}{s(s+\alpha)}$	$1 - a^k$	$\frac{(1-a)z}{(z-1)(z-a)}$
8	$e^{-\alpha t} - e^{-\beta t}$	$\frac{\beta - \alpha}{(s+\alpha)(s+\beta)}$	$a^k - b^k$	$\frac{(a-b)z}{(z-a)(z-b)}$
9	$te^{-\alpha t}$	$\frac{1}{(s+\alpha)^2}$	kTa^k	$\frac{azT}{(z-a)^2}$
10	$\sin(\omega_n t)$	$\frac{\omega_n}{s^2 + \omega_n^2}$	$\sin(\omega_n kT)$	$\frac{\sin(\omega_n T)z}{z^2 - 2\cos(\omega_n T)z + 1}$
11	$\cos(\omega_n t)$	$\frac{s}{s^2 + \omega_n^2}$	$\cos(\omega_n kT)$	$\frac{z[z - \cos(\omega_n T)]}{z^2 - 2\cos(\omega_n T)z + 1}$
12	$e^{-\zeta\omega_n t} \sin(\omega_d t)$	$\frac{\omega_d}{(s + \zeta\omega_n)^2 + \omega_d^2}$	$e^{-\zeta\omega_n kT} \sin(\omega_d kT)$	$\frac{e^{-\zeta\omega_n T} \sin(\omega_d T)z}{z^2 - 2e^{-\zeta\omega_n T} \cos(\omega_d T)z + e^{-2\zeta\omega_n T}}$
13	$e^{-\zeta\omega_n t} \cos(\omega_d t)$	$\frac{s + \zeta\omega_n}{(s + \zeta\omega_n)^2 + \omega_d^2}$	$e^{-\zeta\omega_n kT} \cos(\omega_d kT)$	$\frac{z[z - e^{-\zeta\omega_n T} \cos(\omega_d T)]}{z^2 - 2e^{-\zeta\omega_n T} \cos(\omega_d T)z + e^{-2\zeta\omega_n T}}$
14	$\sinh(\beta t)$	$\frac{\beta}{s^2 - \beta^2}$	$\sinh(\beta kT)$	$\frac{\sinh(\beta T)z}{z^2 - 2\cosh(\beta T)z + 1}$
15	$\cosh(\beta t)$	$\frac{s}{s^2 - \beta^2}$	$\cosh(\beta kT)$	$\frac{z[z - \cosh(\beta T)]}{z^2 - 2\cosh(\beta T)z + 1}$